A RAKE PROCESSOR
FOR THE
IDENTIFICATION OF
FADING COMMUNICATION CHANNELS

A thesis submitted
in partial fulfilment of the requirements
for the degree of
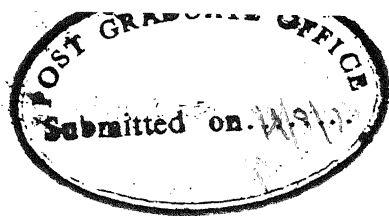MASTER OF TECHNOLOGY IN ELECTRICAL ENGINEERING

by

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to the

DEPARTMENT OF ELECTRICAL ENGINEERING
INDIAN INSTITUTE OF TECHNOLOGY, KANPUR
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CERTIFICATE

Certified that this work, 'A RAKE Processor for the Identification of Fading Communication Channels' by Mr. L. Sudhakara Rao has been carried out under my supervision and that this has not been submitted elsewhere for a degree.

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CONTENTS

SYNOPSIS

The characterization and identification of fading communication channels such as a Troposcatter channel are usually a pre-requisite for using the medium for signal transmission by optimal modem techniques to combat multipath fading characteristics exhibited by such channels. A fading communication channel can often be adequately characterized by a linear system with an equivalent low-pass impulse response that is a complex Gaussian process.

(i) RAKE technique involves the use of wide band signalling at the transmitter and correlation reception at receiver as an anti-multipath measure over fading communication channels. By using correlation detection technique, the transmitted signal arriving with different time delays can be isolated. RAKE concept may also be applied for probing the Troposcatter channel to get estimates of channel response for different time delays.

Though the impulse response function $g(t, \xi)$ of the channel is considered as continuous in both time, t and delay variable, ξ it can be considered ~~for~~ from practical point of view to be not finer than the inverse of the bandwidth, B of the sounding signal for identifying its estimates for different time delays. In view of the above, the fading channel can be represented by a tapped-delay line with number

of taps equal to the number of discrete paths with tap
spacing corresponding to 1/B which is referred to as multi-
path resolution. In such a tapped-delay line, the incoming
signal appears at the input of delay line and after weightages
called tap-gain functions which are random processes, the sum of
the tap outputs constitutes the received signal at the receiver.

For anti-multipath signalling, a wide band-pass
noise-like waveform such as PN sequence is a useful continuous
signal structure. The waveform is a random process and a
moderately long segment of such sequence exhibits preferable auto-
correlation properties. Also, for cross-correlation purpose
at receiver, an exact replica is available.

For channel response identification, the shifted
replicas of the transmitted signal are generated for different
values of time delays and then cross-correlated with the
received signal. Because of the correlation property of the
transmitted PN sequence, the outputs of the cross-correlators
give the direct measure of apparent channel response at
relative time delays.

(ii) The objective of the present system is to obtain
the estimates of randomly varying quadrature components of
channel response function for different time delays and then
investigate the fluctuations caused by fading in signal
phase and signal amplitude. At the transmitter, for probing

the medium, PN sequence of period $(2^{15}-1)$ is chosen by which the 60 MHZ IF is phase-shift keyed at 10 M bauds and then filtered to 10 MHZ bandwidth to be transmitted over Troposcatter channel. At receiver, the received signal is split into in-phase and quadrature components which are cross-correlated with identical binary streams each of which is delayed by 0.1 μsec with respect to the preceding one. This provides a multi-path resolution of 0.1 μsec. The outputs of the cross-correlators give the estimates of the randomly varying quadrature components of channel response function for different time delays.

(iii) The hardware realization of a part of the receiver system as shown in block diagram of Fig.3.0 includes the addition of Gaussian noise of 10 MHZ bandwidth and centred at 60 MHZ to the incoming 60 MHZ IF signal, splitting of the signal into in-phase and quadrature components followed by extraction of the video components and conversion of the positive or negative going signal into digital '1' or '0' in polarity sensing detectors.

CHAPTER - 1

INTRODUCTION

1.0 TROPOSCATTER AS A COMMUNICATION CHANNEL:

The Troposphere is the region of earth's atmosphere extending from ground to a height of about 10 KM. The turbulent air motion and water content cause variations in the refractive index of Troposphere from point to point as well as in time. In one model, the changes in refractive index are grouped in 'blobs' in earth's atmosphere which represent refractive indices different from that of the surrounding medium. This abrupt change in refractive index causes a 'scattering' of EM wave and thus the energy is re-radiated towards the earth by blob. The scatter radiation comes from the large number of scatterers within the volume common to both transmitting and receiving antenna beams.

Troposcatter provides (a) multichannel service over distances of 100 KM to 1000 KM, (b) good spectrum utilization and (c) high degree of security.

1.1 NEED FOR IDENTIFICATION OF CHANNEL CHARACTERISTICS:

Characterization and identification of fading communication channels are normally required for using such media for transmitting signals by optimal modem techniques. In this section, the nature of propagation

vagaries like fading and multipath are described which demand channel characterization.

Considering the transmission of continuous tone (carrier) from the transmitter, let n be the number of blobs contributing to the received signal which can be treated as a random variable. Also, the amplitude $A_i(t)$ and phase $\phi_i(t)$ of the received signal from each of these blobs can be treated as random variables.

In terms of random phasors, the resultant amplitude, $R(t)$ and phase, $\Theta(t)$ of the signal at receiver antenna can be represented by

$$R(t)\, e^{j\Theta(t)} = \sum_{i=1}^{n} A_i(t)\, e^{j\phi_i(t)} \qquad (1.1)$$

Considering independently varying large number of random phasors, the values of the quadrature components of the resultant at any instant are uncorrelated and approach independently as Gaussian variables. The resulting sum at any instant has the characteristics of a narrow band-pass Gaussian noise with Rayleigh fading envelope and uniformly distributed phase. In Eq. (1.1), the amplitude of the resultant signal $R(t)$ has Rayleigh distribution and phase $\Theta(t)$ is uniformly distributed over $(0, 2\pi)$.

$$p_R(r) = \frac{r}{\sigma^2} \ e^{-r^2/2\sigma^2} \qquad , \quad r \geq 0$$

$$p_\Theta(e) = 1/2\pi \qquad , \quad 0 \leq \Theta \leq 2\pi$$

Where σ^2 is the variance of independent and identically distributed zero-mean normal random variables, $X(t)$ and $Y(t)$ (real and imaginary components of phasor $R(t) \ e^{j\Theta(t)}$).

To introduce a more quantitative expression to the channel descriptions above, it is necessary to characterize the channel response function and discuss covariance functions in statistical model of fading.

1.2 CHARACTERIZATION OF TROPOSCATTER CHANNEL:

The tropochannel may be characterized as a linear time-varying band-pass filter whose impulse response varies stochastically as a Gaussian process. If $Z(t)$ is the complex low-pass signal input and $g(t,\xi)$ is the complex equivalent low-pass impulse response of such filter, then the complex low-pass signal output can be represented as

$$w(t) = \int_{-\alpha}^{\alpha} g(t,\xi) \ z(t-\xi) \ d\xi \qquad (1.2)$$

If short term fading characteristics exhibit Rayleigh distribution, then $g(t,\xi)$ and hence $w(t)$ is a zero-mean complex Gaussian process in t with its quadrature components having the same variance for each t. If $z(t) \longleftrightarrow z(f)$,

$$z(t-\xi) = \int_{-\alpha}^{\alpha} z(f) \ e^{j2\pi f(t-\xi)} \ df \qquad (1.3)$$

Letting $g(t,\xi) \longleftrightarrow T(t,f)$, from Eqs.(1.2) and (1.3),

$$w(t) = \int_{-\alpha}^{\alpha} T(t,f) \; z(f) \; e^{j2\pi ft} \, df \qquad (1.4)$$

where $T(t,f)$ is the time-variant transfer function of the channel and is also a zero-mean complex Gaussian process.

Correlation functions:

The Tropo-channel can adequately be characterized by atleast 2nd order statistical functions the measurement of which requires that the process should be atleast wide-sense stationary over time intervals of the order of measurement time.

Considering the mean of $g(t,\xi)$ as zero and $g(t,\xi)d\xi$ as the complex gain associated with path delays in the interval $(\xi,\xi+d\xi)$, the correlation function $Q(\xi,\eta,\tau)$, is called Tap-gain or Path-gain Correlation function or Multipath Time-covariance function of WSS channel.

$$Q(\xi,\eta,\tau) = \overline{g^{*}(t,\xi) \; g(t+\tau,\eta)} \qquad (1.5)$$

For a WSS channel which also exhibits uncorrelated scattering (WSSUS), $Q(\xi,\eta,\tau)$ has the form

$$Q(\xi,\eta,\tau) = Q(\xi,\tau) \; \delta(\xi-\eta)$$

$Q(\xi,0)$ is called the Delay power spectrum or Multipath intensity profile. For WSSUS channels, scattering function $S(\xi,\upsilon)$ is defined as

$$S(\xi,\upsilon) = \int Q(\xi,\tau) \; e^{-j2\pi\upsilon\tau} \, d\tau \qquad (1.6)$$

$S(\xi, \vartheta)$ describes the relative intensity of all scatterers involving a propagation path of relative delay ξ and having a Doppler Shift ϑ.

1.3 PROPOSED SCHEME OF CHANNEL RESPONSE IDENTIFICATION:

1.3.1 Introduction:

In this section, a tapped-delay-line representation for the channel has been discussed. The impulse response function of the channel, $g(t,\xi)$ is considered as containing a continuous multipath structure over a continuum of values of ξ. Practically, this continuum working is impossible. However, we can expect that the detail considered for estimating $g(t,\xi)$ need not be finer than 1/B where B is bandwidth of the sounding signal.

The signal received over a fading multipath channel can be represented as

$$w(t) = \int_{-\alpha}^{\alpha} g(t,\xi) \; z(t-\xi) \; d\xi \qquad (1.7)$$

where $w(t)$ and $z(t)$ are the complex envelopes of the received and transmitted waveforms respectively and $g(t,\xi)$ is the time-varying equivalent low-pass impulse response of the channel. Variations of $g(t,\xi)$ as t varies are slow so that the dependence of $g(t,\xi)$ on ξ can be found by means of sounding signal.

1.3.2 Tapped-delay-line representation for the channel:

Let the complex envelope of the transmitted signal, $z(t)$ has a 2-sided spectrum such that $-\frac{B}{2} \leq f \leq \frac{B}{2}$. From sampling theorem, $z(t)$ can be expressed as

$$z(t) = \sum_{j=-\alpha}^{\alpha} z(j/B) \; (\sin \pi B(t-j/B)/\pi B(t-j/B))$$

(1.8)

From Eqs. (1.7) and (1.8), it can be shown that

$$w(t) = (1/B) \sum_{j=-\alpha}^{\alpha} g_1(t,j/B) \; z(t-j/B),$$

(1.9)

where $g_1(t, j/B)$ is an equivalent low-pass time varying impulse response for the channel corresponding only to its low-pass transfer function over $-B/2 \leq f \leq B/2$. Only that portion of the channel response which is relevant to transmitted signal confinement of $|f| < B/2$ is considered.

For signals bandlimited to B, it is enough if the behaviour of the channel is estimated in terms of effective impulse response $g_1(t, \xi)$ at intervals spaced $1/B$ apart in ξ. Letting $g_1(t, j/B) = g_j(t)$, the channel model implied by Eq. (1.9) is given within dotted lines of Fig.1.1.

1.3.3 Channel response identification:

The present scheme of identifying the channel response is the use of wideband signalling and correlation

reception as an antimultipath measure over fading channels. For sounding the channel, a wide band-pass noise-like waveform (PN sequence) is a useful continuous signal structure. An exact replica is also available as cross-correlation reference and a moderately long segment of such sequence exhibits autocorrelation properties. Let a segment of length T of PN sequence be used as sounding signal over interval $0 < t \leq T$ $(T \gg 1/B)$.

The estimates of $g_j(t)$ can be obtained by extracting an identical T-length segement of the replica process available at receiver, delaying it by K/B and cross-correlating it against the received signal, $w(t)$. Letting $j/B = \xi_j$ and $K/B = \eta_k$, the output of cross-correlator may be given as

$$s_k(t) = \int_{\eta_k}^{T+\eta_k} w(t) \; z^*(t-\eta_k) \, dt$$

$$= 1/B \sum_{j=-\alpha}^{\alpha} g_j(t) \int_{\eta_k}^{T+\eta_k} z^*(t-\eta_k) z(t-\xi_j) dt \qquad (1.11)$$

If $T \gg 1/B$, we can assume that the finite length integral can be well approximated by its average over ensemble of all possible T-length segments of $z(t)$.

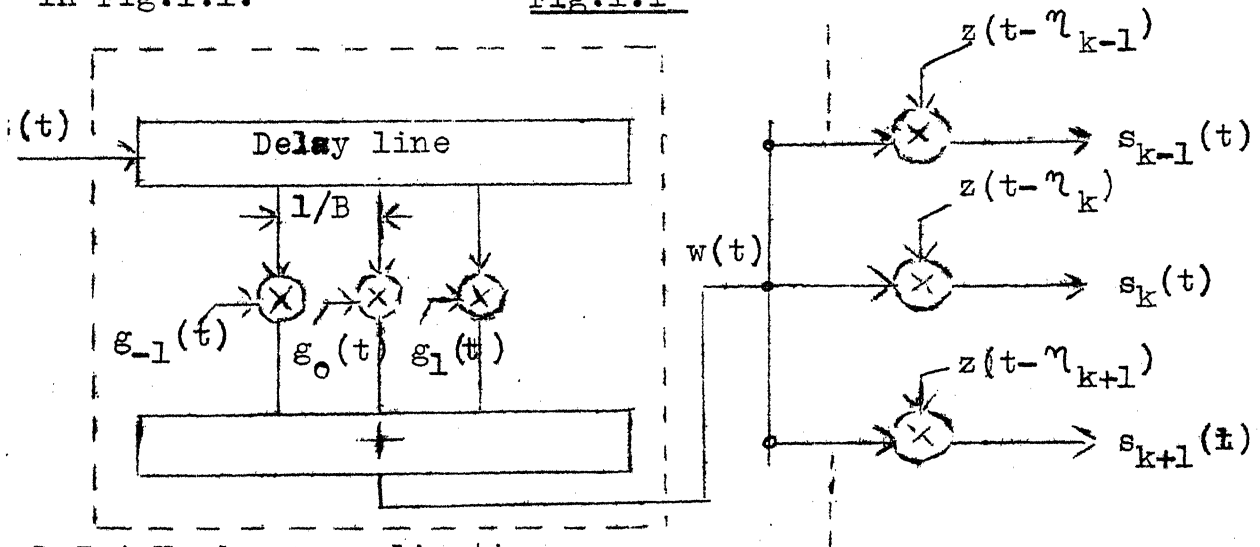$$\phi(\xi) = 1/T \int_0^T z^*(t) \; z(t+\xi) \, dt \qquad (1.12)$$

From Eqs. (1.11) and (1.12),

$$s_k(t) = T/B \sum_{j=-\alpha}^{\alpha} g_j(t) \, \phi_z(\eta_k - \xi_j) \qquad (1.13)$$

Whenever $\eta_k = \xi_j$, $s_k(t)$ is maximum because of choice of $z(t)$. Thus the output of cross-correlator, $\phi_z(o) \, g_j(t)$ is the estimate of $g_j(t)$. So, the correlation with reference relatively delayed by $\eta_k = K/B$ selects only that part of the arriving signal energy represented by Kth tap in the tapped delay line model of the channel.

The block diagram implied by the tapped-delay - line model of multipath fading channel and correlation reception to measure channel response for different time delays is shown in Fig.1.1.

Fig.1.1

1.3.4 Hardware realization:

The block diagram shown in Fig.3.0 represents the designed and fabricated part of the receiver system. The incoming 60MHZ IF signal is added with locally generated Gaussian noise of 10 MHZ bandwidth and centred at 60 MHZ so

as to maintain required S/N ratio to linearize the polarity sensing process. It is then fed to two multipliers the other inputs of which being the quadrature components of local 60 MHZ IF which is in phase with the transmitted IF. Thus, the incoming signal is split into normal (in-phase) and quadrature components. The outputs of the multipliers are passed through low pass filters to extract the video components which are amplified by video amplifiers to be fed to polarity sensing detectors represented by difference-amplifier and comparator circuits. The output of a polarity sensing detector is a logical '1' or '0' for positive or negative going signal component.

The resulting in-phase and quadrature components of the incoming signal are to be cross-correlated with the time-shifted replicas of the transmitted signal (PN sequence) to get estimates of channel impulse response function for different time-delays.

1.4 OUTLINE OF VARIOUS CHAPTERS:

Chapter 1 gives a brief discussion of fading troposcatter channel characteristics followed by tapped-delay line model of representing channel and the proposed scheme of channel response identification.

Chapter 2 mostly deals with functional system block diagram based on the technique of channel response identification as discussed in Chapter 1.

Chapter 3 contains starting with block diagram of the fabricated part of the proposed system, both a description and the design of different circuits involved.

Chapter 4 gives information about printed cards and mechanical construction and layout details of the boxes alongwith description and purpose of the provided controls.

In Chapter 5, a brief description of tests carried out and the experimental results obtained have been given.

CHAPTER - 2

SYSTEM DESCRIPTION[10,11,12]

2.0 INTRODUCTION:

RAKE technique of wideband signelling and correlation reception is used for communication over fading channels. This technique can also be used for probing the troposcatter channel to get an estimate of channel scattering function.

2.1 RAKE SYSTEM DESCRIPTION:

2.1.1 System Objective:

The objective of the system is to record randomly varying in-phase and quadrature components of channel response function, $g(t, \xi)$ as it varies both in ξ and t and analyse the data obtained to provide an estimate of the channel scattering function.

2.1.2 System Characteristics:

(a) Operating frequency .. 2-1 GHZ

(b) Transmission technique .. AM

(c) IF frequency .. 60 MHZ

(d) Sounding Signal .. PN sequence (period= $2^{15}-1$)

(e) Method of signal modulation .. PS Keying at 10 Mega bauds

(f) Signal bandwidth .. 10 MHZ

(g) Multipath resolution .. 0.1 μ sec.

(h) Order of diversity 15

(i) Diversity technique ...... Multipath

(j) Detection technique .... Correlation

(k) Mode of propagation .. Single hop, overland scatter

(l) Test-link range ... 300 miles

(m) Integration time .. millisec.
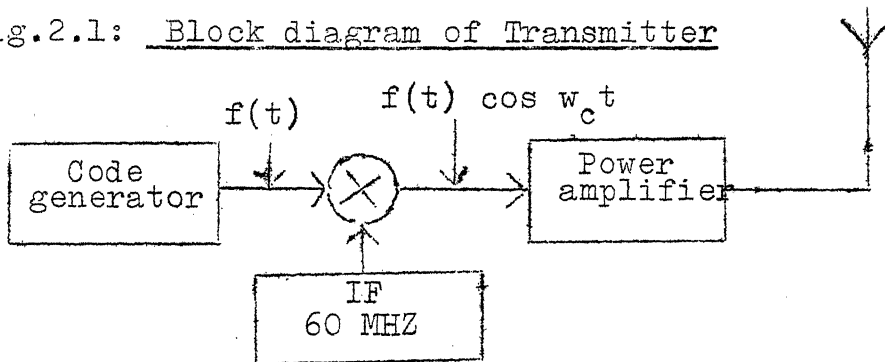
2.1.3 Signalling:

To probe the medium for its impulse response, wideband signalling is required. Pulses of very short duration are unsuitable as the repetition rate cannot be made low enough to keep the observed response from over-lapping in time due to limitation of peak power than can be transmitted. However, a wideband noise like waveform i.e., Pseudo-Noise sequence (PN Seq.) serves as an excellent continuous signal structure. It contains sufficient details so that the waveform at one instant of time can be distinguished from that at another instant of time (since, at zero time-lag, auto-correlation = 2^M-1 and at time lags of one or more elements, auto-correlation = 0 or unity where M is the number of stages in shift register generating PN sequence).

2.1.4 Simplified block diagram of Transmitter:

The code generator in Fig.2.1 is a 15-stage shift register connected with feedback for maximal length code generation. The IF is 60 MHZ phase-shift keyed at 10 M bauds by PN sequence, filtered to 10 MHZ bandwidth and then power

amplified to be transmitted over a tropospheric path.

Fig.2.1: <u>Block diagram of Transmitter</u>

2.1.5 Block diagram of Receiver:.

Block diagram of RAKE receiver is shown in Fig.2.2.
The transmitted signal is corrupted with additive white
gaussian noise and arrives at the receiver sequentially via
different paths of the illuminated common volume of the
troposcatter medium.

The multiplied output of frequency synthesizer
is used as receiver local oscillator. The resultant 60 MHZ
IF signal of 10 MHZ BW serves as an input to the signal
attenuator stage of RAKE demodulator.

Locally generated gaussian noise with 10 MHZ
BW and centred at 60 MHZ is added to IF signal so as to
maintain required S/N ratio to linearize the polarity sensing
process (see section 2.2).

The signal is then fed to IF amplifier the output
of which is injected into two multipliers of normal and
quadrature channels. The quadrature components of the
locally derived 60 MHZ IF which is in phase with transmitted
IF serve as other inputs to the multipliers.

The low-pass filters recover the required normal and quadratic components of sounding signal by eliminating the high frequency content of multiplier outputs.

The video outputs are then amplified and fed to polarity sensing detectors (PSD). Each PSD is strobed by 10 MHZ master clock and at the moment of strobing, PSD output is a logical '1' or '0' depending upon whether the input signal is positive or negative in polarity.

The receiver contains a shift register to generate a PN Seq. which is identical and in synchronism with the one used at the transmitter. Synchronization of PN sequence can be provided in the synchronous sweep circuit.

The shift register provides 15 time-shifted and sequenced local copies of transmitted PN code which are cross-correlated with the sampled normal and quadratic components of received signal in 30 mod-2 adders to get a continuous estimate of amplitude and phase for each particular delay/tap.
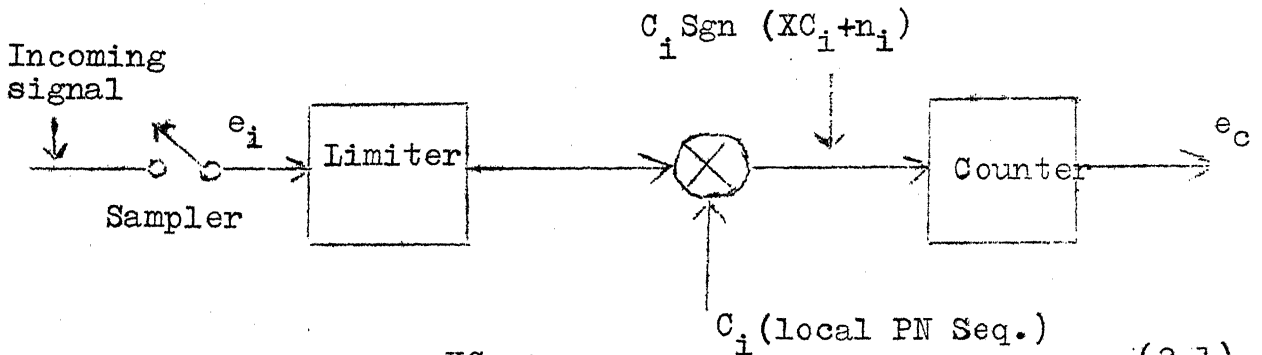
The storage counter provided for each tap accumulates the information of how many times the signal and code sequence correlate during each integration period. At the end of integration period, storage counter is reset to zero after its selected number of active bits are transferred into a buffer register.

The outputs of buffer register are then multi-plexed and recorded on a digital tape recorder for computer processing.

2.2 QUANTIZATION AND SAMPLING[10]:

The one-bit quantization or limiting of the input samples will introduce an error causing nonlinearity between the average counter output and input signal component. Anyhow, the amount of error can be minimized by adding an appropriate amount of Gaussian noise to the received signal. Let e_i be the output of the sampler and input to one of the quadrature quantizers and e_c, the output of the counter as shown in Fig.2.3.

Fig. 2.3

$$e_i = XC_i + n_i \tag{2.1}$$

$$e_c = \sum_{i=1}^{N} C_i \, Sgn \, (XC_i + n_i) \tag{2.2}$$

where   X= one quadrature component of channel gain at one particular delay and is assumed constant over an integration period,

C_i = transmitted PN sequence = ± 1,

n_i = samples of (a) received noise and

(b) signals with delays differing by more

than a bit period of PN seq. which is

negligible,

$$\text{Sgn}(XC_i + n_i) = \begin{cases} = +1 \text{ for } (XC_i + n_i) \text{ positive} \\ -1 \text{ for } (XC_i + n_i) \text{ negative} \end{cases}$$

By carrying out multiplication process before limiter,

Eq.(2.2) is mathematically equivalent to

$$e_c = \sum_{i=1}^{N} \text{Sgn}(X + n_i') = \sum_{i=1}^{N} \text{Sgn}(X + n_i) \qquad (2.3)$$

where n_i' has same properties as n_i,

X is constant over integration period,

$$\text{Sgn}(X + n_i) = \begin{cases} +1 \text{ with probability } P \\ -1 \text{ with probability } (1-P) \end{cases}$$

$$P = \text{Pr}[X > -n_i] = \left[1/\sqrt{2\pi}\sigma \right] \int_{-X}^{\alpha} e^{-y^2/2\sigma^2} dy$$

$$= \tfrac{1}{2} + (1/\sqrt{2\pi}) X/\sigma \text{ for small S/N ratio} \quad (2.4)$$

(i.e., $X \ll \sigma$) at limiter

using Eqns. (2.3) and (2.4),

(a) Mean of counter output, : $\overline{e}_c = N\sqrt{2/\pi}\, X/\sigma$ \qquad (2.5)

Eq.(2.5) ensures linearity of counter output to input

signal component by adding an appropriate amount of

Gaussian noise to the received signal preceding the limiter

and sampler.

(b) With constant signal and independent noise from sample to sample, variance of counter output, $\sigma_c = N.$ (2.6)

(c) RMS S/N ratio of counter output, $(S/N)_c = \sqrt{2N/\pi} \cdot (X/\sigma)$

(2.7)

2.3 DATA ANALYSIS:

The outputs of cross correlators or RAKE taps can be considered as a set of estimates of $g_j(t)$ where g is a complex number (phasor) represented by normal (in-phase) and quadrature components of tap output and j identifies the tap being considered.

Considering n observations and taking sample mean i.e., time averaging over a finite time of experiment, tap-gain correlation and scattering functions for different time delays/taps can be computed using Eqns. (1.5) and (1.6).

CHAPTER 3

CIRCUIT DESCRIPTION AND DESIGN

3.0 INTRODUCTION:

In this chapter, the operation and hardware realization of the various circuits used are discussed. Except where considered necessary, the discussion has been limited to a brief presentation of the salient features.

A functional block diagram of the designed and fabricated part of the system is shown in Fig.3.0.

The incoming 60 MHZ IF signal corrupted with additive White Gaussian Noise constitutes the input signal with a bandwidth of 10 MHZ.

The binary sequences at normal and quad. output terminals are further processed in the digital correlator and counting circuits to obtain the estimates of the fading channel characteristics.

3.1 SIGNAL ATTENUATOR [1,2,5]

3.1.1 INTRODUCTION:

Conventional attenuators (i.e. ladder network and electronic attenuator using emitter follower) may be unsuitable at very high frequencies without good quality contact switches. Moreover, neutralization of stray and wiring capacitances may pose problems in these cases.

However, an FET used as a voltage controlled resistor (VCR) can serve as an excellent signal attenuator[1]. Such an attenuator can have a large dynamic range and adjustable bandwidth.

An FET in the region where the drain-source voltage V_{DS} is approximately zero may be shown[17] for any reverse bias V_{GS} between 0 and V_p to have a small signal drain-to-source resistance r_d to be a function of V_{GS} given by

$$r_d(V_{GS}) = r_d(0)/(1-K V_{GS})$$

where V_{GS} is the gate-source voltage,

$r_d(0)$ is the drain-to-source resistance at

$V_{GS} = 0$ and

K is a constant dependent upon FET type

Thus, by controlling V_{GS}, a variable voltage-controlled resistor may be obtained.

3.1.2 CONFIGURATION SELECTION:

Of the two commonly used configurations shown in Figs.3.1 and 3.2, configuration-B is favoured as configuration-A has the following disadvantages.

(a) The output of VCR has to be terminated into a 50-ohm load. As VCR appears in the low side of the attenuator,

Fig.3.0 : Block Diagram of fabricated part of the system

Fig. 3.2: CONFIGURATION-B

Fig. 3.1: CONFIGURATION-A
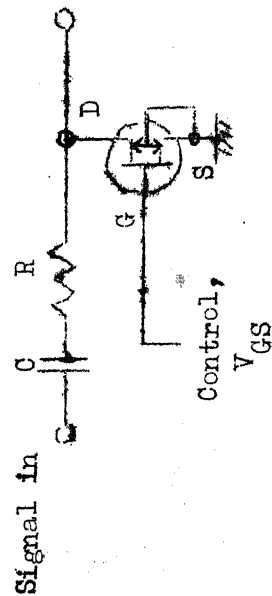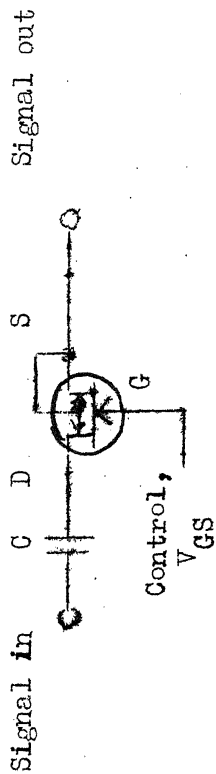
the following stage should have a very high input

impedance.

(b) There is 180º phase shift between input and output.

(c) The input signal level should be high.

3.1.3 CIRCUIT CONFIGURATION:

The circuit configuration used for signal attenuation

at 60 MHZ range using FET is shown in Fig.3.3 and the equivalent

high-frequency model is given in Fig.3.4.

Fig.3.3   Circuit Configuration

Fig.3.4:   Equivalent high-frequency model of Fig.3.3

C_{in} and L_1 resonate at 60 MHZ

C_{out} and L_2 resonate at 60 MHZ

V_{GS} is the test voltage

3.1.4 DESIGN OBJECTIVES:

3.1.4.1   Frequency of operation   :   60 MHZ

3.1.4.2   Band-width   :   15 MHZ

3.1.4.3   Input impedance   :   50 ohms

3.1.4.4   Output impedance   :   50 ohms

3.1.4.5   Control voltage range, V_{GS}:   0 to -5 volts

3.1.4.6   Voltage attenuation range :   -15 dB

3.1.4.7   Supply voltage available :   -12V

3.1.5 DESIGN CONSIDERATIONS:

3.1.5.1   A straight forward analysis of the equivalent

circuit in Fig.3.4 would show that

$$R_{out} \approx R_2 \left\| \frac{1}{g_m} \right. \qquad \text{for } r_d \gg R_1$$

$$C_{out} = C_2 + C_{gs} + C_{ds}(\mu+1) + C_{stray}$$

$$R_{in} \simeq R_1 \qquad \text{for } r_d \gg R_1$$

$$C_{in} = C_1 + C_{gd} + \frac{C_{gs}}{\mu+1} + C_{stray}$$

3.1.5.2 Conditions to be satisfied:

(a) For R_{out} to be less dependent on g_m variations, R_2 should be as small as possible when compared to $\frac{1}{g_m}$.

(b) For R_{out} to be less dependent on r_d variations, R_1 should be as small as possible when compared to r_d.

Therefore, both R_1 and R_2 should be chosen as small as possible so as to keep R_{out} to be less dependent on g_m and r_d variations which occur due to varying V_{GS}. In such case,

$$R_{out} \simeq R_2 \quad \text{and}$$

$$R_{in} \simeq R_1$$

3.1.6 SELECTION OF DEVICE AND COMPONENTS

3.1.6.1 Device chosen is Junction FET, type BFW10, n-channel.

Typical characteristics of BFW10 are as given in Appendix-A.

3.1.6.2 Resistors: $R_1 = R_2 = 180$ ohms

3.1.7 CIRCUIT DESIGN:

Centre frequency, fo $= 60$ MHZ

Bandwidth, B $= 15$ MHZ

$$W_0 = 2\pi f_0 = 6.3 \times 60 \times 10^6 = 3.78 \times 10^8 \text{ radians}$$

$$\frac{1}{W_0} = 2.645 \times 10^{-9} \text{ rad}^{-1}$$

$$\text{Loaded Q of tank circuit, } Q_L = \frac{f_o}{B} \qquad (3.1)$$

$$= \frac{60}{15} = 4$$

3.1.7.1 Input Network:

Fig.3.5

Source resistance, R_S = 50 ohms

$$R_{in} = R_1 = 180 \text{ ohms}$$

Total capacitance shunting $L_1 = C_{in} = C_1 + C_{stray} + C_{gd} + \frac{C_{gs}}{\mu+1}$

R_S is reflected as 180 ohms onto the right hand side of L_1 and across R_1. Therefore, for impedance matching, the effective resistance shunting L_1 is

$$R_1' = \frac{R_1}{2} = \frac{180}{2} = 90 \text{ ohms}$$

$$L_1 = \frac{R_1'}{W_o Q_L} \qquad (3.2)$$

$$= \frac{90 \times 2.645 \times 10^{-9}}{4} \approx 0.06 \, \mu H$$

For single-layer solenoids of the proportions normally used in radio work, the inductance is given to an accuracy of about 1 percent by an approximate formula[6]

$$L = \frac{n^2 r^2}{9r + 10l} \, \mu h \qquad (3.3)$$

where   L is the inductance in microhenries

r is the radius of coil (inches) between the centres
of conductors

n is the number of turns

l is the length of the coil (inches) i.e., n times
the distance between centres of adjacent turns.

For $n = 4$ Turns,

$r = 0.276"$ (7 mm) and

$l = 0.4"$,

$\therefore \quad L \simeq 0.06 \, \mu h.$

Total capacitance across L_1 is $C_{in} = \dfrac{1}{W_o^2 \, L_1} \qquad (3.4)$

$$\approx \; 115 \; pf.$$

Therefore, external capacitance required across L_1 is

$$C_1 = 115 - (C_{stray} + C_{gd} + \frac{C_{gs}}{\mu + 1}) \; pf$$

Experimentally, C_1 is determined and found to be 97 pf

To find tap on L_1:

$$\frac{n_S}{n_1} = \sqrt{\frac{R_S}{R_1}} \qquad ; \qquad \therefore n_S = n_1 \sqrt{\frac{R_S}{R_1}} \qquad (3.5)$$

$$= 2 \text{ turns from ground}$$

3.1.7.2 Output Network:

<u>Fig. 3.6:</u>

C_{out} & R_{out}

$$R_{out} = R_2 = 180 \text{ ohms}$$

$$C_{out} = \text{Total capacitance across } L_2$$

$$= C_2 + C_{stray} + C_{gs} + C_{ds}(\mu+1)$$

$$L_2 = 0.06 \mu h$$

$$n_2 = 4 \text{ turns}$$

$$n_L = 2 \text{ turns from ground}$$

$$C_{out} = 115 \text{ pf}$$

$$C_2 = 115 - (C_{stray}+C_{gs}+C_{ds}(\mu+1)) \text{ pf}$$

Experimentally, C_2 is determined and found to be 120 pf.

3.1.7.3 Circuit Diagram:

Signal Attenuator circuit diagram with component values is given in Fig.3.7.

Fig.3.7: Circuit Diagram of Signal Attenuator

3.1.8 CONSTRUCTION:

3.1.8.1   As with most high frequency circuits, careful mechanical layout is necessary to minimize the coupling between the input and output stages. The components with very short leads have been used to minimize stray inductance. The input and output tank circuits have been shielded effectively from the device and the biasing circuit and the signal attenuator block itself has been inturn shielded from the rest of the circuitry. Component wiring has been printed on an epoxy glass printed board to minimize the signal losses.

3.1.8.2   Signal level control facility has been provided. Signal level can be monitored by adjusting R_4 by mean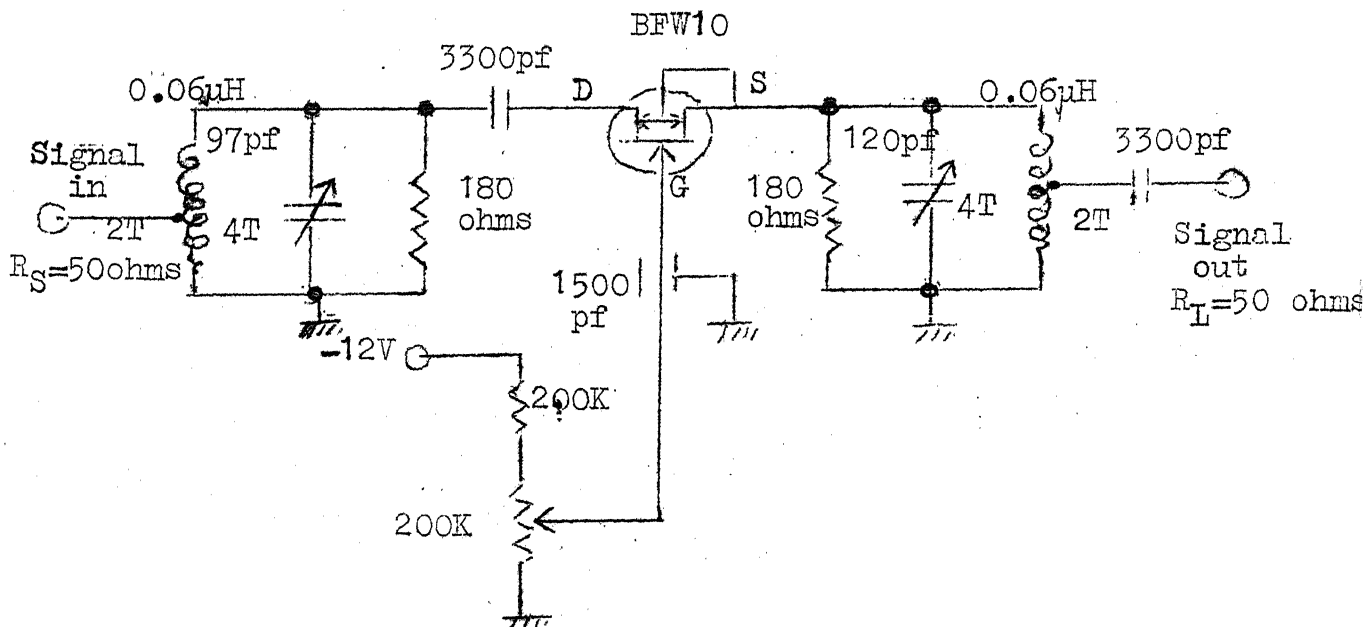s of which the negative voltage applied to the gate of the device varies which in turn alters the degree of attenuation of the signal.

3.1.9 PERFORMANCE:

          The circuit performance is measured at different frequencies for different gate voltages. The results are given in Table 3.1 and the circuit response in the curve. This performance is shown as a function of $-V_{GS}$, negative voltage applied to the gate of the device for different frequencies.

Table: 3.1   EXPERIMENTAL OBSERVATIONS

Level of Input signal to the attenuator = 320 mV (unloaded)
160 mV (loaded)

Gate control Voltage, V_{GS} in Volts	Output of Attenuator in millivolts at			Signal Attenuation in dB at		
	55 MHZ	60 MHZ	65 MHZ	55 MHZ	60 MHZ	65 MHZ
0	32.5	40	32.5	-13.8	-12	-13.8
-0.5	31	38	31	-14.3	-12.5	-14.3
-1.0	28	35	28.5	-15.1	-13.2	-15
-1.5	27	33	27	-15.5	-13.7	-15.5
-2.0	23.5	29.3	23.5	-16.6	-14.7	-16.6
-2.5	21.5	27	21.5	-17.4	-15.5	-17.4
-3.0	17	21.8	17.3	-19.5	-17.3	-19.3
-3.5	10.8	14	11	-23.4	-21.2	-23.3
-4.0	3.3	4.2	3.3	-33.7	-31.6	-33.7
-4.5	2.8	3.8	2.8	-35.1	-32.5	-35.1
-5.0	2.8	3.8	2.8	-35.1	-32.5	-35.1

SIGNAL ATTENUATOR

V_{GS} vs Freq. curves for 55, 60 & 65 MHZ

Gate control, V_{GS} Volts

Signal Attn. in dB

60 MHZ

55 & 65 MHZ

3.2 NOISE GENERATOR[3,4]

3.2.1 INTRODUCTION:

Commercial noise sources have used thyratron kept in transverse magnetic field as the basic source of noise current In the present system, however, a reverse biased p-n junction is used.

3.2.2 DESIGN SPECIFICATIONS:

The noise source is intended to meet the following specifications:

3.2.2.1 Output Spectrum: 3dB points, 51 and 69 MHZ

3.2.2.2 Output level   : Variable from 2 mV to 10 mV   p-p

3.2.2.3 Output impedance: 50 ohms

3.2.3 NOISE GENERATION TECHNIQUE[3]

In the case of reverse biased p-n junction, reverse current, I may be expressed as

$$I = MI_O$$

where I_O is the theoretical reverse current

and M is the multiplication factor given by

$$M = \frac{1}{1 - (\frac{V_a}{V_{br}})^m}$$

where V_a is the applied voltage,

V_{br} is the breakdown voltage

and $m \simeq 3$ for silicon and n-type germanium

The reverse breakdown voltage, V_{br} is a function of doping levels. If $V_{br} > 7V$, the diode is said to breakdown in avalanche mode. In the transition region, the high current discharges are called as microplasma. It is found that this gives rise to random noise current in the device. These avalanche breakdown microplasmas occur preferentially where dislocations pass through the junction.

3.2.4 CIRCUIT CONFIGURATION[4]:

3.2.4.1 Noise Generator:

Fig.3.8 shows a simple arrangement which exploits the above phenomena. R_2 is used to vary the reverse current, I_R to bias the zener diode near the knee and the noise voltage is developed across R_3.

Microplasma - noise generation takes place only in a certain range of diode currents, $I_1 < I < I_2$ where I_1 and I_2 depend upon the surface properties of device and vary from unit to unit. The output amplitude of the noise varies if the bias changes in the above range.

The amplitude probability distribution of stationary Gaussian noise current is described by

$$P(X) = \frac{1}{\sqrt{2\pi}\,\sigma} \exp (X-m)^2 \Big/ 2\sigma^2$$

where
σ = rms value of the current

m = mean value of the current

X = random noise current

From this, it can be deduced that the instantaneous noise voltage lies within $\pm 3\sigma$ for 99.7 percent of time. Thus an amplifier used to provide noise output of σ volts rms must be able to handle the instantaneous peaks of $\pm 3\sigma$ volts if significant errors due to overloading are to be avoided.

Fig.3.8:   Wide band noise source:

$-12V$

3.2.4.2 Biasing:

The device chosen is SZ213 the reverse breakdown voltage, V_{br} of which is about 8.2 volts. At the transition region where microplasma phenomena occurs, the reverse current is found to be about 30 to 40 μa. R_2 is adjusted to achieve this. R_1 is chosen so as to draw a maximum reverse current of 2ma when $R_2 = 0$.

3.2.4.3 Noise Amplifier:

A two-stage common-base tuned amplifier has been used to boost the noise output developed across R_3 to get the

Fig.3.9: CIRCUIT DIAGRAM OF NOISE GENERATOR AND AMPLIFIER

required noise level with specified noise output spectrum. The tank circuits of the two stages of the amplifier are stagger-tuned to get the required bandwidth. The stages are identical to those in IF amplifier block described later. The complete circuit diagram of noise generator and amplifier block is shown in Fig.3.9.

3.3 LINEAR ADDITION OF SIGNAL AND NOISE[5]

3.3.1 INTRODUCTION:

Linear addition is the process of combining two or more signals from different sources into one composite signal. Basic characteristics of linear addition are given below.

(a) Signals from one source should not appear at any of the other sources i.e., there must be good isolation between the output and input sections of the circuitry.

(b) No additional frequencies or distortion should be added by the circuitry.

3.3.2 COMMON-EMITTER TO COMMON-BASE CASCODE CIRCUIT:

The circuit diagram using IC3028A with common-emitter to common-base cascode arrangement is shown in Fig.3.10. The two advantages obtained from the cascode arrangement of CE to CB stages are given below.

(a) There is a minimum of internal feedback from the output to the input terminal. Voltage swings at

the collector of Q_2 will couple the energy back thro'
C_{bc_2} to its base and be bypassed through C_B to the
ground. Voltage swings at the collector of Q_1 are
developed across the low-input resistance of Q_2. The
$g_n R_L$ multiplier for C_{bc_1} will be low and superior high
frequency performance can be expected. This reduced
internal feedback makes it possible to have a tuned
circuit for a load without incurring oscillations.

(b) The output voltage swing can be large. When both
transistors Q_1 and Q_2 are near saturation, V_O
approaches the voltage across C_E or V_E. When both Q_1
and Q_2 are near cut-off, V_O approaches V_{CC}. Therefore,
the total peak-to-peak output voltage swing is
nearly $(V_{CC}-V_E)$.

Fig.3.10: Common-emitter to Common-base cascode circuit

.3 <u>CIRCUIT CONFIGURATION</u>:

The schematic diagram for linear addition of the incoming signal and the locally generated noise is shown in Fig.3.12. IC type CA3028A has been employed for CE to CB cascode arrangement. Manufacturer's specifications of CA3028A have been given in Appendix-A. Two cascode circuits are used one for each of the two signals to be added and the addition process is carried out by mixing the signal currents from both Q_2 and Q_2' in coupling resistor, R_C shunted by the output tank circuit and the input resistance of IF amplifier stage. The inductance coil of the tuned circuit is tapped down to feed R_L of 30 ohms load which is the input resistance of the following IF amplifier stage.

In the schematic diagram, the digits 2 to 6 refer to the terminal numbers of CA3028A. S_1 indicates the incoming signal, S_2 the locally generated noise and R_L the input resistance of the following IF stage.

The collectors of Q_2 and Q_2' offer good isolation between the two channels (i.e., signal and noise). The fact that the output impedances R_{o1} and R_{o2} at the collector terminals of Q_2 and Q_2' (CB configuration) are very high when compared to the effective load, $R_C' = \dfrac{R_C}{2} = 75$ ohms ensures excellent isolation between the two channels.

.3.4   <u>CIRCUIT DESIGN</u>:

.3.4.1 Biasing:

I_{C1} and I_{C2} are the collector currents of Q_2 and Q_2' of the two cascode circuits. The biasing resistors are chosen so as to make each of them equal to 5 ma. Total current, I_C flowing through common collector resistor of 150 ohms will be 10 ma. The dc voltages appearing at the terminals of CA3028A are shown in Fig.3.12.

.3.4.2 Output network: Collector of Q_2

<u>Fig.3.11</u>

R_{out} in cascode arrangement is very high when compared to R_C of 150 ohms. Therefore, the resistance shunting L is 150 ohms.

Centre frequency, f_o = 60 MHZ

Band width chosen, B = 20 MHZ

Therefore, $Q_L = \dfrac{f_o}{B} = 3$

Using equations 3.1 to 3.5,

L = 0.066 μh (d=0.35", l=0.6", n_c=4 turns)

C = 105 pf

n_L = 1.75 turns from ground.

FIG.3.12: CIRCUIT DIAGRAM OF LINEAR ADDITION OF SIGNAL AND NOISE

3.4   IF AMPLIFIER[7,8,9]

3.4.1 INTRODUCTION:

Narrow band amplifiers are characterized by frequency discrimination and provide large gain over a specified band-width. Such amplifiers are generally tuned amplifiers using resonant circuits to obtain desired selectivity and centre frequency.

3.4.2 DESIGN METHODS:

In IF amplifiers, the internal feedback of the device causes the transistor input impedance to be a function of load impedance which makes the multistage IF amplifier alignment difficult. Design methods to overcome the internal feedback effects are

(a) Neutralization method and

(b) Mismatching method

Neutralization method is to neutralize the effect of the reverse feedback ratio or unilateralize the transistors in the amplifier. This technique is usually limited to a narrow-band, high gain applications.

Mismatching method involves mismatching the device at its input and output terminals. The advantages of this method are given below.

(a) Stability for all devices of particular type.

(b) Useful stable gains upto very high frequencies

(c) Easy practical multistage amplifier alignment.

Mismatching technique has been chosen for IF and Noise amplifier stages as it suits the requirements of stable gain at high frequencies and over wideband.

3.4.3 DESIGN SPECIFICATIONS:

3.4.3.1 Centre frequency, f_o = 60 MHZ

3.4.3.2 Overall Band-width, B = 10 MHZ

3.4.3.3 Voltage gain, V_G = 35 dB

3.4.3.4 Input and output impedances = 50 ohms each

3.4.3.5 Design method = Mismatching technique

3.4.4 CIRCUIT DESIGN:

3.4.4.1 The device chosen is 2N918, silicon, NPN type, Fairchild transistor. The manufacturer's specifications for 2N918 are given in Appendix A.

For common-base configuration at I_C = 4ma, V_{CE} = 6 V and f_o = 60 MHZ, the input and output impedances are as given below:

Input resistance, R_{ib} = 30 ohms

Input inductance, L_{ib} = 0.05 μh

Output resistance, R_{ob} = 2.5 K ohms

Output capacitance, C_{ob} = 4 pf

The circuit diagram is given in Fig.3.13. Three stages of common-base mode have been used.

3.4.4.2 Bandwidth per stage:

Overall half power bandwidth for n identical stages in terms of the single stage band-width is given by the expression

$$B = B_S \ (2^{1/n} - 1)^{1/2} \simeq \frac{B_S}{1.2n} \qquad (3.6)$$

where   B is the overall bandwidth of n cascaded stages,

B_S is the band-width of individual, identical stages,

n is the number of stages.

For 3-stage IF amplifier, n=3 and $B = 0.5B_S$

For B = 10 MHZ, B_S = 20 MHZ

∴ Bandwidth per stage = 20 MHZ

Loaded Q of each tank circuit, $Q_L = \frac{f_o}{B_S} = \frac{60}{20} = 3$

3.4.4.3 Input network of the 1st stage:

Signal in

R_S=50 ohms

C_O

R_{E1}

2.7K

○Emitter of Q_1

$\rightarrow \begin{cases} R_{in_1} = 30 \ \text{ohms} \\ L_{in_1} = 0.05 \ \mu H \end{cases}$

It is decided to resonate L_{in_1} with C_O at 60 MHZ and allow slight mismatch between R_S and R_{in_1} which improves the stability of the amplifier. In any case, the amount of mismatch can be reduced or controlled by proper adjustment of the tap on the output tank circuit of the preceding stage (i.e., Linear

addition of signal and noise) from which the signal is fed

to the input network of the 1st stage of IF amplifier.

$$C_o = \frac{1}{W_o^2 \, L_{in_1}} \qquad = \quad \frac{2.645^2 \times 10^{-18}}{0.05 \times 10^{-6}} \quad = \quad 140 \text{ pf}$$

Allowing for stray and wiring capacitances, $C_o = 130$ pf.

3.4.4.4 Output network of last (3rd) stage:

Resistance shunting $L_3 = R_{o_3} \parallel R_{c_3} = 2.5 \text{ K} \parallel 1.5\text{K} = 940$ ohms

From equations 3.1 to 3.5, we get for $Q_L = 3$,

$L_3 = 0.4 \mu h$ ($l = 0.4"$; $d = 0.55"$; $n_3 = 6$ turns)

Total capacitance across L_3, $C = 18$ pf $= C_{o_3} + C_3$

Therefore, $C_3 = 14$ pf

$n_L = 1.5$ turns from ground (for $R_L = 50$ ohms)

$= 1$ turn from ground (for $R_L = 30$ ohms)

L_3 and C_4 resonate at a frequency nearly 5 times lower than

60 MHZ. Choosing resonant frequency of 5 MHZ,

$C_4 = 0.0033 \mu F$

3.4.4.5 Interstage coupling network:

Proceeding on the same lines as given under clause

Collector of Q1

$R_{o1}=2.5K$
$C_{o1}=4pf$

R_C 1.5K

C_1

n_1

L_1

n_2

3300pf

Emitter of Q2

$L_{i_2}=0.05\mu H$

$R_{i_2}=30$ ohms

3.4.4.5, the chosen value of $L_1 = 0.4\mu h$. $L_{i_2}=0.05\mu h$ is reflected as $2\mu h$ onto the left hand side of L_1 and the effect of it has been neglected in the calculations.

$$C_1 = 14 \text{ pf},$$

$$n_1 = 6 \text{ turns, and}$$

$$n_2 = 1 \text{ turn from ground}$$

3.4.4.6 Mid-band voltage gain:

Overall mid-band voltage gain of 3-stage Amplifier is

$$\frac{V_L}{E_S} = \left(\frac{\beta_o}{\beta_o+1}\right)^3 \frac{R_o \sqrt{R_o R_L}}{R_i (R_S+R_i)} = 73.3 = (37 \text{ dB})$$

where R_o is the output resistance of CB stage,

R_i is the input resistance of CB stage,

R_S is the source resistance and

R_L is the load resistance.

3.4.5 CONSTRUCTION:

Careful mechanical layout has been carried out to minimize parasitic inductance and capacitance. Transistor sockets can be used even at these frequencies because small capacitances are not as important as low lead-inductance.

Component leads are cut as short as possible to minimize stray inductance. The output network of each stage is shielded well from its input network. The output of IF amplifier is available through an IF connector, type UG 291/U which is fixed to the box.

3.4.6   PERFORMANCE:

The experimental observations of the IF amplifier are given in Table 3.2 and the performance is shown as a function of frequency in the response curve. These gain measurements were based with

(a) a 50 ohm source and a 50 ohm load   and

(b) the three stages stagger-tuned to get an overall band-width of 15 MHZ.

Fig.3.13: CIRCUIT DIAGRAM OF IF AMPLIFIER

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TABLE: 3.2   EXPERIMENTAL OBSERVATIONS

Level of Input signal to IF Amplifier, $A_i = \begin{cases} 3.25 \text{ mV p-p (unloaded)} \\ 1.62 \text{mV p-p (loaded)} \end{cases}$

Input signal frequency in MHZ	IF Amplifier output, A_v in mV	Voltage gain	
		A_v/A_i	$20 \log_{10} A_v/A_i$ dB
67	55	33.8	30.5
66	68	42	32.4
65	73	45	33
64	76.5	47	33.5
63	77.6	47.8	33.6
62	79.5	48.9	33.8
61	80	49.2	33.8
60	80	49.2	33.8
59	79.3	48.8	33.7
58	77.5	47.8	33.6
57	76	46.7	33.4
56	71.5	44.4	33
55	66	40.6	32.2
54	60	37	31.3
53	54	33.2	30.4

IF AMPLIFIER

Voltage gain vs. frequency
response curve

3 dB Freqs. : 53.2 & 66.8 MHZ
Bandwidth : 13.6 MHZ

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3.5   MULTIPLIER[13,5]

3.5.1 INTRODUCTION:

In this section, a single differential pair employed as a multiplier for normal and quadratic channels has been discussed. The incoming modulated signal (S_1) forms one of the inputs to both multipliers while the other input (S_2) is the local 60 MHz IF which is in phase with the transmitted IF for normal channel and 90° out of phase for quadratic case. To avoid any interaction between the multipliers, there must be good isolation between input and output sections of each multiplier.

3.5.2 CIRCUIT ANALYSIS:

3.5.2.1   The differential pair multiplier configuration is shown in Fig.3.14. The circuit gives good isolation between the output and input sections.

For S_1, Q_1-Q_2 combination acts as CC to CB cascode arrangement and there is no phase shift between S_1 and V_o. External resistor at collector of Q_1 is omitted so that no signal voltage can be developed at collector of Q_1 for coupling back through C_{bc_1} to the base of Q_1. Also, the base of Q_2 is shunted with suitable capacitor, C_B so that any signal voltage fed back from collector of Q_2 through C_{bc_2} will be bypassed to ground. Consequently, the circuit has good high-frequency performance.

For S_2, Q_3-Q_2 combination acts as CE to CB cascode arrangement and there is phase reversal between S_2 and V_o. Voltage swings at collector of Q_2 will couple the energy back through C_{bc_2} to its base and be bypassed to ground through C_B. Also, voltage swings at collector of Q_3 are developed across low-input resistance of Q_2. The low gain and the consequent smaller Miller capacitance of Q_3 ensure improved high-frequency performance.

3.5.2.2 Multiplier Out-put:

Voltage gain of a differential amplifier is readily shown to be proportional to g_m of Q_2 which because of its linear dependence on i_{c_3} can be effectively controlled by S_2. Multiplier output, V_0 in terms of S_1 and S_2 is shown[5] to be

$$V_0 = S_1 (A_1 + A_2 S_2) \qquad (3.7)$$

where

$$A_1 = \frac{I_{c_3} R_c}{0.1} = \left(\frac{V_{B_3} - V_{BE_3}}{R_{E_3}} \right) \frac{R_c}{0.1}$$

and

$$A_2 = R_C/0.1 \left(R_{E_3} + \frac{r_3 + R_B}{\beta_{O_3}+1} \right)$$

Let $S_1(t)$ be the PS keyed signal and $S_2(t)$, the local IF in phase with transmitted IF.

$$S_1(t) = f(t) \cos w_c t \quad \text{and} \quad S_2(t) = \cos w_c t \quad \text{where } f(t) = \pm 1$$

$$V_0(t) = K_1 f(t) \cos^2 w_c t + k_2 f(t) \cos w_c t \qquad (3.8)$$

$$= \frac{k_1}{2} f(t) + \frac{k_1}{2} f(t) \cos 2w_c t + k_2 f(t) \cos w_c t$$

where k_1 and k_2 are constants. If $f(t) \longleftrightarrow F(W)$,

$$V_O(W) = \frac{k_1}{2} F(W) + \frac{k_1}{4}(F(W+2W_c)+F(W-2W_c))$$
$$+ \frac{k_2}{2}(F(W+W_c) + F(W-W_c))$$

The original signal $f(t)$ can be recovered by using a low-pass filter which will allow $F(W)$ to pass and will attenuate the remaining components centred around $\pm 2W_c$ and $\pm W_c$.

3.5.3 CIRCUIT DESIGN:

3.5.3.1 Low pass filter:

The R_c-C_c combination in the collector of Q_2 forms the low-pass filter. Taking into consideration the effect of $R_L = 50$ ohms, total resistance shunting C_c is $R_c \| R_L = 25$ ohms. Choosing cut-off frequency, f_c of 12 MHz,

$$C_c = (1/2\pi f_c)(R_c \| R_L) = 500 \text{ pf.}$$

3.5.3.2 Phase-shifting of Network[16]:

A π-network which introduces a phase lag of 90° is designed to operate at 60 MHz frequency for input and output impedances of 50 ohms each and the circuit diagram is shown in Fig.3.15.

Fig.3.14 : SCHEMATIC DIAGRAM OF MULTIPLIER

S₁ : Incoming modulated signal

S₂ : Local 60 MHZ IF

Fig.3.15 : 90° PHASE SHIFTING NETWORK

3.6 VIDEO AMPLIFIER [7,8,14]

3.6.1 INTRODUCTION:

A stable video amplifier of 10 MHz bandwidth is constructed using shunt-feedback network around each stage. The use of collector-to-base feedback is a method of improving bandwidth which results in reduced (a) input and output impedances and (b) overall gain at low frequencies, trading gain for bandwidth.

3.6.2 DESIGN SPECIFICATIONS:

3.6.2.1   Overall voltage gain, A_V : 35 dB

3.6.2.2   Bandwidth   : 10 MHz

3.6.2.3   Input impedance   : 50 ohms

3.6.2.4   Output impedance   : 50 ohms

3.6.3 DESIGN PROCEDURE: [7]

3.6.3.1 Design Equations:

The following are the design equations for a single-stage collector feedback amplifier.

Input resistance, $R_{in} = r_\pi \left|\right| \dfrac{R_F + R_L}{1 + g_m R_L}$ $\qquad$ (3.11)

Voltage gain, $A_V = -g_m (R_L \left|\right| R_F)$ $\qquad$ (3.12)

Current gain, $A_i = \dfrac{\beta_0 (R_L + R_F)}{r_\pi + R_F + (\beta_0 + 1) R_L}$ $\qquad$ (3.13)

Shunt-feedback resistance, $R_F \approx \dfrac{A_i \, r_\pi + \beta_0 R_L (A_i - 1)}{(\beta_0 - A_i)}$ (3.14)

$$\approx \dfrac{R_{in} \, r_\pi + R_{in} R_L (\beta_0 + 1) - R_L r_\pi}{r_\pi - R_{in}} \quad (3.15)$$

3.6.3.2 DC Biasing:

The Collector current in the last stage should be high enough to provide a high output voltage but the first stage collector current should be low enough to stabilize the input impedance.

3.6.3.3 Design of Shunt-feedback resistance:

Using equations as given under clause 3.6.3.1, the shunt feed-back resistors can be calculated starting from last stage taking into consideration the source and load impedances of 50 ohms each. The table given below gives the calculated parameters.

Amplifier stage	I_C ma	R_L ohms	R_F ohms	R_{in} ohms	A_v	A_i
3	11.4	50	280	10	20	5
2	3.8	10	200	50	1.5	8
1	1.9	50	300	50	3	4

Overall mid-band voltage gain, $A_v = 39.$ dB

where

R_L : Load/output resistance

R_F : Collector feedback resistance

R_{in} : Source/Input resistance

3.6.3.4 Emitter bypassing and coupling:

Electrolytic capacitors of 250 μF in parallel with polyester type of 0.022 μF have been used for both bypassing and coupling. The leads of capacitors are trimmed to minimum to reduce the effective series inductance.

3.6.3.5 Decoupling:

With very low input and output impedances of each stage, very little signal current flows through collector resistor to be coupled back into collector supply voltage lead. Also, with each emitter bypassed to ground, very little signal current flows through the emitter resistor. Sufficient decoupling is achieved with networks shown in Fig.3.16.

3.6.4 CIRCUIT CONFIGURATION[14]

The circuit configuration of video amplifier is shown in Fig.3.16. Capacitance coupling has been employed as the amplifier may suffer from operating point stability with direct coupling. The device chosen is silicon, NPN transistor, type 2N3563 having f_T of 600 MHz and β_F of 20.

3.6.5 PERFORMANCE:

The performance of the video amplifier with resistive shunt feedback arrangement is observed with source and load impedances of 50 ohms each. The 3-dB low-and high-frequencies have been observed to be about 70 HZ and 15 MHZ respectively.

With transistors of low f_T, R-L feedback may have to be used for all the stages except the first one for good overall high frequency response and the first stage should have resistive feedback to provide a flat-input-impedance character-istic[7].

3.7 POLARITY SENSING DETECTOR[15,5]

3.7.1 INTRODUCTION:

A symmetrical transistor amplifier followed by a difference-amplifier comparator has been used to serve as polarity sensing detector (PSD) with one of the inputs connected to ground (reference voltage) while the other measuring input to the signal. Comparator output assumes one of the two levels i.e., digital "1" or "0" for positive or negative going input signals.

3.7.2 CIRCUIT CONFIGURATION:

The schematic diagram of PSD is shown in Fig.3.17. The difference amplifier is highly stable because of the nature

Fig.3.16: CIRCUIT DIAGRAM OF VIDEO AMPLIFIER

Q_1, Q_2, Q_3: 2N3563

Table 3.3 EXPERIMENTAL OBSERVATIONS (Video Amplifier)

Level of Input signal, $v_{in} = \begin{cases} 12 \text{ mV} & \text{(unloaded)} \\ 6 \text{ mV} & \text{(loaded)} \end{cases}$

Input signal freq.		Video Amp. o/p, v_{out} in mV	$\dfrac{v_{out}}{v_{in}}$	$\dfrac{v_{out}}{v_{in}}$ in dB
10	MHZ	320	53.3	34.5
8	"	330	55	34.8
6	"	338	56.3	35.0
4	"	344	57.3	35.2
2	"	348	58.0	35.3
1	"	350	58.3	35.3
800	KHZ	350	58.3	35.3
600	"	350	58.3	35.3
400	"	350	58.3	35.3
200	"	365	60.8	35.7
100	"	375	62.5	35.9
80	"	375	62.5	35.9
60	"	375	62.5	35.9
40	"	380	63.3	36.0
20	"	385	64.2	36.1
10	"	400	66.7	36.5
8	"	400	66.7	36.5
6	"	400	66.7	36.5
4	"	395	65.8	36.4
2	"	395	65.8	36.4
1	"	400	66.7	36.5
800	HZ	400	66.7	36.5
600	"	400	66.7	36.5
400	"	390	65.0	36.3
200	"	380	63.3	36.0
100	"	330	55.0	34.8
80	"	300	50.0	34.0
60	"	250	41.7	32.4
20	"	120	10.0	20.0

of the device, IC CA3028A used.

3.7.3 CIRCUIT DESCRIPTION:

When the input signal, v_i to the difference amplifier goes sufficiently positive by a few milli-volts, Q_3 should turn ON to detect the crossing of zero reference in the positive direction. Conversely, when Q_3 turns OFF, output goes to 0 volts to indicate that the input has crossed zero in negative direction.

3.7.3.1 DC Analysis:

At balance, the input voltage, $v_i = 0$ and the dc voltages at different terminals are shown in Fig.3.17. Resistance R is adjusted so that Q_3 is in active region so that the voltage at the collector of Q_3 i.e., $v_{out} = + 2.5$ volts.

3.7.3.2 Q_3 TURN ON:

With v_i crossing zero sufficiently in positive direction such that the $Q_{11}-Q_{12}$ develops a minimum differential output voltage that is sufficient to cut-off Q_{21} and drive Q_{22} into saturation, $v_{0+} = V_{CC}-7$ ma x 0.47 K ohms = + 1.7V and Q_3 is driven into saturation. Thus, $v_{out+} = + 5$ volts (digital "1").

3.7.3.3 Q_3 TURN OFF:

With v_i crossing zero sufficiently in negative direction, Q_{21} becomes ON and Q_{22} goes into cut-off state resulting in $v_{0-} = + 5$ volts. Thus, Q_3 is OFF and $v_{out-} = 0V$ (digital "0").

v_i	Q_{21}	Q_{22}	v_0	Q_3	v_{out}
0	Active	Active	+3.3V	Active	+ 2.5V
+ve	OFF	ON	+1.7V	ON	+ 5V (digital "1")
-ve	ON	OFF	+5V	OFF	0V (digital "0")

3.7.3.4 Minimum Crossing Voltage:

(a) Considering difference-amplifier comparator circuit (Q_{21}, Q_{22}), total range of output swing, Δv_0 overwhich the output can follow the input is

$$\Delta v_0 = I_{E_{23}} R_{C_2} = 7ma \times 0.47 \text{ k ohms} = 3.3V \text{ p-p}$$

Differential voltage gain, $A_d = \dfrac{\Delta v_0}{\Delta v_i} = \dfrac{g_m R_{C_2}}{2}$ from which the total input voltage swing required is $\Delta v_i = 100$ mv p-p.

(b) Considering difference-amplifier circuit (Q_{11}, Q_{12}), $\Delta v_0 = 100$ mv p-p and $A_d = \dfrac{\Delta v_0}{\Delta v_i} = g_m R_C$ from which $\Delta v_i = 3$ mv p-p.

Thus, total input voltage swing required at the input of difference amplifier to carry the output of the comparator through its entire swing of 3.3 V p-p is 3 mV p-p.

3.7.4 OBSERVATIONS:

The PSD is tested with a sine wave input of 50 HZ to 10 MHZ. Total input voltage swing required at the difference-amplifier to carry the output of the comparator stage through

its entire swing is observed to be about 10 mV p-p.
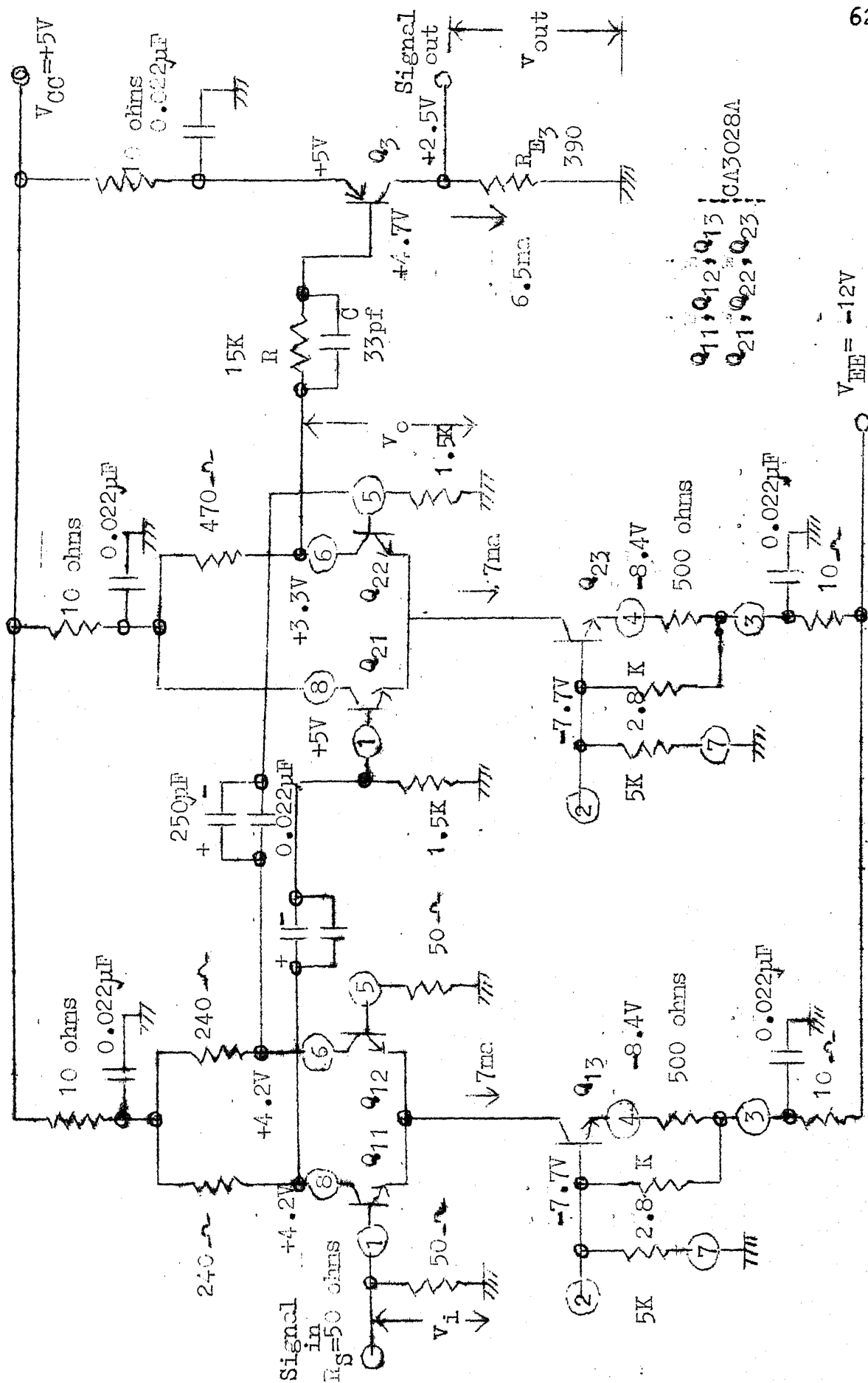
       With input signal level of about 50 mV p-p, the output of PSD approaches a step waveform satisfactorily throughout the frequency range of 50 HZ to 10 MHZ.

Fig.3.17: SCHEMATIC DIAGRAM OF POLARITY SENSING DETECTOR

CHAPTER - 4

MECHANICAL CONSTRUCTION AND LAYOUT

In this chapter, brief mechanical construction of housing of the printed cards and the controls have been described.

4.0 PRINTED CARDS:

The distribution of 10 printed cards of 7 types used are given below:

Sr.No.	Description	No. of cards used
1.	Signal attenuator	1
2.	Noise generator and amplifier	1*
3.	Linear addition of signal and noise	1
4.	IF amplifier	1*
5.	Multiplier	2**
6.	Video amplifier	2**
7.	Polarity sensing detector	2**

* The printed card has noise generator followed by a 3-stage tuned amplifier circuitry. For noise generator and amplifier at Sr.No.2, the 3rd stage of tuned amplifier has been discarded while for IF amplifier at Sr.No.4, the noise generator circuitry has not been used.

** Two sets of printed cards are used for normal and quadrature channels. In printed card against Sr.No.5, a 90° phase

shifting network is incorporated which is used for quadrature channel case only.

4.1 MECHANICAL CONSTRUCTION AND LAYOUT:

Printed cards against Sr.Nos.1 to 4 are housed in BOX-1 for convenience of monitoring noise and signal levels either individually or combined at IF amplifier output. The rest of the printed cards are mounted in BOX-2. The printed cards are mounted on bottom plate through spacers and fitted with screws at the bottom. The side plates cover the boxes on four sides and the middle plates shield the different printed cards. The top plate completes the structure of the box and can be fitted onto the side plates. The layouts of printed cards in Boxes-1 and -2 are shown in Figs. 4.1 and 4.2.

4.2 CONTROLS:

The controls on the boxes are mounted onto the front (side) plate. Description and purpose of controls are given below:

4.3.1 BOX-1: (Fig.4.1)

4.3.1.1 SW-1: It is NOISE ON/OFF switch, DPST in ON (up) position of which noise can be added to signal and in OFF (down) position, noise generator can be disconnected.

4.3.1.2 P-1 : They are noise and signal level control
&
        P-2   potentiometers respectively.

4.3.1.3 FTC-1 They are feed-through capacitors through which
&
        FTC-2 +12 and -12 V supplies can be fed.

4.3.1.4 C-1   They are female connectors used for feeding
&
        C-2   and obtaining the input and output signals

                respectively.

4.3.2 BOX-2: (Fig.4.2)

4.3.2.1. C-3   It is a female connector through which the signal

                (from IF amplifier output of BOX-1) can be fed

                to multipliers.

4.3.2.2. C-4   It is a female connector through which the

                local 60 MHZ IF can be fed to the multipliers.

4.3.2.3 FTC-3,5 They are feed-through capacitors through which
        FTC-4 &
        FTC-6 +5, +12 and -12V supplies respectively can be fed.

4.3.2.4 FTI-1   They are feed-through insulators from which the
&
        FTI-2   normal and quadrature components of the received

                signal can be obtained.

4.3.2.5 FTI-3   They are feedthrough insulators through which
        and
        FTI-4   10 MHZ clock for strobing PSDs can be fed.
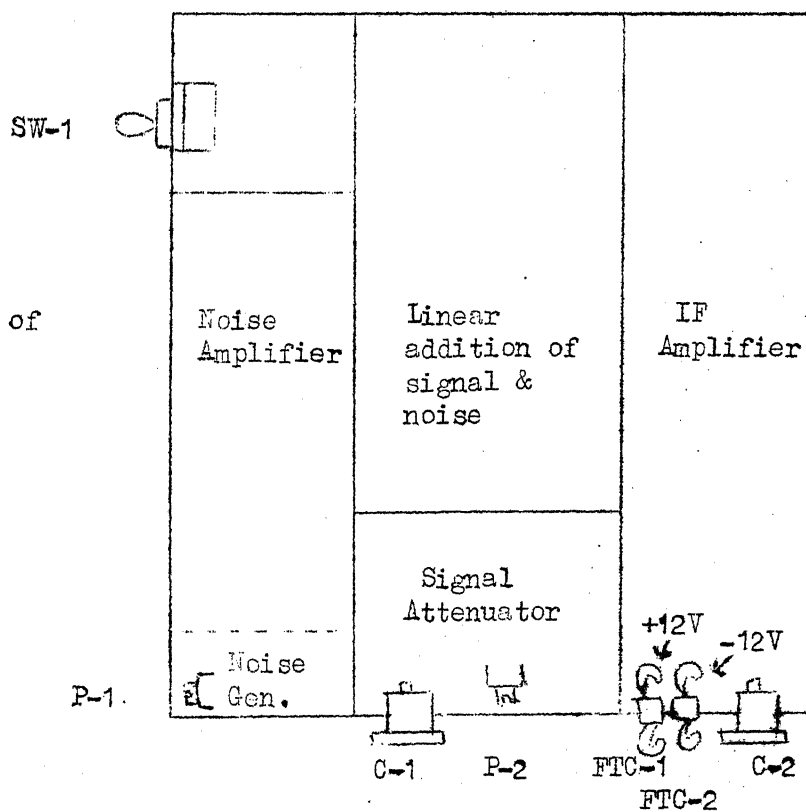
Fig. 4.1 : Layout of BOX-1

Fig. 4.2 Layout of BOX-2

CHAPTER 5

PERFORMANCE MEASUREMENT AND CONCLUSIONS

In this chapter, a brief description of the tests conducted on the two boxes and the experimental results along with response curves have been given.

5.1 Box-1: (Fig.4.1)

With final stagger-tuning of all the coupled stages, the frequency response of Signal stages constituting the signal attenuator, addition stage and IF amplifier and that of Noise stages comprising noise amplifier, addition stage and IF amplifier have been measured.

(a) Table 5.1 shows the experimental results for Signal stages as obtained with signal applied to signal attenuator and noise generator disconnected. The output is observed at the output of IF amplifier terminated into a 50-ohm load.

(b) Table 5.2 shows the results for Noise stages as observed with signal attenuator and noise generator disconnected and signal applied to noise amplifier. The observations are carried out at the output of IF amplifier terminated into a 50-ohm load.

(c) With noise generator connected, the noise level at the IF amplifier output is found to be variable from a

Table 5.1: FREQUENCY RESPONSE OF SIGNAL STAGES

Source impedance, $R_S = 50$ ohms

Gate control voltage of signal attenuator, $V_{GS} = 0V$

Input signal level, $v_{in} = 48$ mV (unloaded)

24 mV (loaded)

Input signal Freq. in MHZ	IF amp. output, v_{out} in mV	$\dfrac{v_{out}}{v_{in}}$	$\dfrac{v_{out}}{v_{in}}$ in dB
66	127	5.3	14.5
65	147	6.1	15.7
64	160	6.7	16.5
63	173	7.2	17.2
62	181	7.5	17.6
61	185	7.7	17.7
60	185	7.7	17.7
59	185	7.7	17.7
58	183	7.6	17.6
57	175	7.3	17.3
56	160	6.7	16.5
55	145	6.0	15.6
54	125	5.2	14.3

Centre frequency : 60 MHZ

3dB corner frequencies: 54.2 & 65.8 MHZ

Bandwidth : 11.6 MHZ

Table 5.2 FREQUENCY RESPONSE OF NOISE STAGES

Source impedance, R_S = 50 ohms.

Input signal level, v_{in} = 11mV (unloaded)

5.5 mV (loaded)

Input signal Freq. in MHZ	IF amp.output v_{out}, in mV	v_{out}/v_{in}	v_{out}/v_{in} in dB
67	250	45.6	33.2
66	320	58.1	35.3
65	370	67.2	36.6
64	390	70.8	37.0
63	410	74.5	37.4
62	420	76.4	37.7
61	420	76.4	37.7
60	420	76.4	37.7
59	420	76.4	37.7
58	420	76.4	37.7
57	400	72.6	37.2
56	380	69.1	36.8
55	350	63.6	36.1
54	310	55.0	34.9

Centre frequency —: 60 MHZ
3 dB corner frequencies : 54 & 66.2 MHZ
Bandwidth : 12.2 MHZ

FREQUENCY
RESPONSE CURVE
OF SIGNAL stages

Bandwidth =11.6 MHZ

IF Output in dB

17.8 dB

17

16

15   14.8 dB

14   54.2 MHZ   65.8 MHZ

55 56 57 58 59 60 61 62 63 64 65 66 67 68

Freq. in MHZ

Freq. response curve
of noise stages

Bandwidth =12.2MHZ

IF output in dB

38   37.7 dB

37

36

35   34.8 dB

34   54.0 MHZ   66.2 MHZ

54 55 56 57 58 59 60 61 62 63 64 65 66 67

Freq. in MHZ

minimum of 10 mV to a maximum of 50 mV peak-to-peak.

5.2 BOX-2:

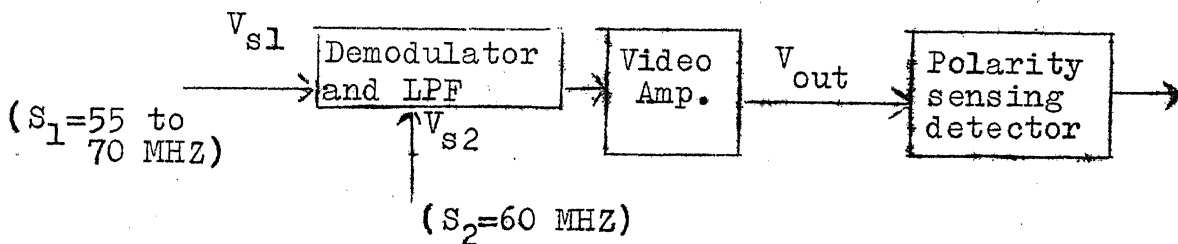A brief description of the tests carried out with reference to the block diagram of Fig.5.1 is given below:

Fig.5.1

V_{s1}

$(S_1=55$ to 70 MHZ)

```
Demodulator and LPF  →  Video Amp.  → $V_{out}$ →  Polarity sensing detector →
```

↑V_{s2}

$(S_2=60$ MHZ)

(a) Single differential-pair multiplier using CA3028A as demodulator:

Testing of Box-2 is carried out by applying 60 MHZ signal to the voltage-gain controlling S_2-input (see 'Multiplier', section 3.5) and 55 to 70 MHZ variable frequency signal to the differential S_1-input of the multiplier stage from two different VHF oscillators. V_{s1} and V_{s2} are the voltage levels of S_1 and S_2 respectively and the voltage levels of the video component after amplification are observed as V_{out} for different frequencies of S_1 ranging from 55 to 70 MHZ in steps of 2.5 MHZ. The results are tabulated in Table 5.3 from which it is observed that (since the video amplifier is found to have bandwidth of 10 MHZ) the differential pair multiplier using CA3028A has bandwidth limitation of 5.7 MHZ.

Table 5.3

V_{s1} = 120 mv S_1=55 to 70 MHZ

V_{s2} = 275 mv S_2=60 MHZ

S_1	55 MHZ	57.5 MHZ	60 MHZ	62.5 MHZ	65 MHZ	67.5 MHZ	70 MHZ
V_{out}	400 mv	470 mv	520 mv	465 mv	390 mv	290 mv	250 mv

(b) Double balanced mixer (Ring demodulator) using
     DBM-1 (ANIDUS make)

The differential-pair multiplier using CA3028A is replaced by double balanced mixer (Ring demodulator) and with the experimental set-up as shown in Fig.5.1, the observations are made at the output of the demodulator. The results are tabulated in Table 5.4 showing the better performance of the ring demodulator over that of differential pair multiplier.

Table 5.4

V_{s1} = 250 mv S_1 = 55 to 70 MHZ

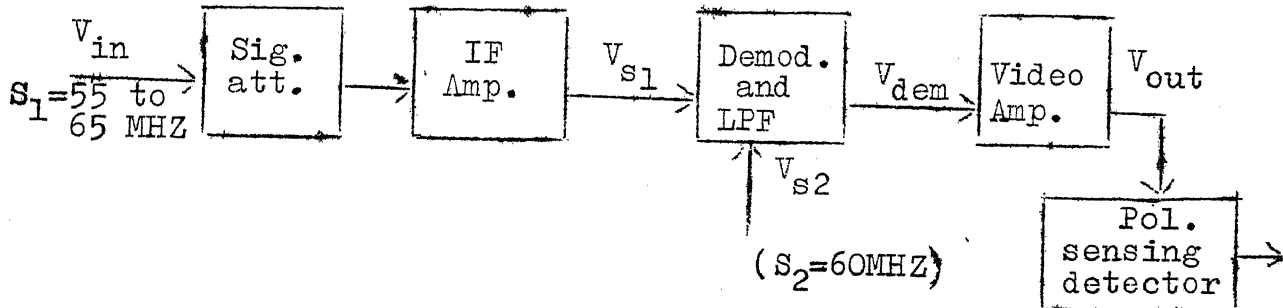V_{s2} = 500 mv S_2 = 60 MHZ

S_1	55 MHZ	57.5 MHZ	60 MHZ	62.5 MHZ	65 MHZ	67.5 MHZ	70 MHZ
Demod. output	200 mv	200 mv	200 mv	200 mv	200 mv	195 mv	190 mv

5.3 Testing of the overall fabricated part constituting Boxes-1 and -2 is carried out, the description of which with reference to block diagram of Fig.5.2 is given below.

Fig.5.2

The signal S_1 of variable frequency from 55 to 65 MHZ is applied to the signal attenuator and the IF amplifier output is coupled to the demodulator, the other input of which being S_2 of 60 MHZ

V_{in} : Level of input signal S_1 to signal attenuator

V_{s1} : IF amplifier output

V_{s2} : Level of S_2

V_{dem} : Level of video component at the demodulator output

V_{out} : Video amplifier output

(a) The response of Box-1 under loaded conditions is measured as a function of frequency. The experimental results are given in Table 5.5 and the corresponding V_{s1} vs freq. plot in Fig.5.3 showing the IF amplifier output V_{s1} for different frequencies of S_1 ranging from 55 to 65 MHZ.

The bandwidth of signal stages (signal attenuator, addition stage and IF amplifier) under loaded conditions is found to be 10 MHZ.

<div align="center">Table 5.5</div>

$$V_{in} = 60 \text{ mv}$$

S_1 in MHZ	65	63	61	60	59	57	55
V_{s1} in mv	198	232	250	257	255	238	204

(b) Differential-pair multiplier using CA3028A as demodulator:

Voltage levels of the video component V_{out} at the video amplifier output are measured for different frequencies of S_1 ranging from 55 to 65 MHZ in steps of 2 MHZ. The results are tabulated in Table 5.6 from which it may be concluded that the differential pair multiplier using CA3028A limits the bandwidth of the fabricated part of the system to 3MHZ. The plot of V_{out} vs. frequency is shown in Fig.5.4.

<div align="center">Table 5.6</div>

S_1 : 55 to 65 MHZ S_2 : 60 MHZ

V_{in} = 60 mv V_{s2}= 360 mv

S_1 in MHZ	55	57	59	60	61	63	65
V_{out} in mv	75	97	126	137	126	99	78

(c) The observations made with double balanced mixer are recorded in Table 5.7 showing the bandwidth of the system to be more than 10 MHZ (about 12 MHZ). The frequency response curve is plotted in Fig.5.5.

Table 5.7

V_{in} = 60 mv $\qquad$ V_{s2} = 1.2v

S_1 in MHZ	55	57	59	60	61	63	65
V_{dem} in mv	200	240	255	260	250	235	195

5.4 LIMITATIONS:

(a) Noise level control is not sensitive.

(b) Differential pair multiplier limits the bandwidth of the system to 3 MHZ.

(c) High-frequency rejection at the demodulator output is poor.

5.5 SPECIAL FEATURES:

(a) Signal Attenuator using FET as a voltage-controlled resistor provides (i) continuous attenuation range and (ii) flexibility of band-width adjustment with suitable drain and source resistances shunting the input and output tank circuits respectively.

(b) Tunability to various frequencies:

With proper stagger-tunning of the tuned circuits,

the fabricated part can be used for operation with IF
frequency of any value between 60 MHZ with overall
bandwidths of signal and noise stages being 10 MHZ each.

(c) Bandwidth of the video Amplifier can be increased
(to about 20 MHZ) without any high-frequency peaking networks.

5.6 SUGGESTIONS FOR IMPROVEMENTS:

(a) An attenuator stage (similar to that used for signal
attenuation) at the output of noise amplifier provides a
fine control of noise level.

(b) A calibrated meter/indicator (at the output of IF
amplifier) facilitates the monitoring of signal and noise level

(c) CE-to-CB cascode circuits between each multiplier
and IF amplifier gives better isolation between the input
and outputs of multiplier stages.

(d) A double balanced mixer (A ring demodulator) type
DBM-1 (ANIDUS make) in the place of single differential-pair
multiplier using CA3028A gives required overall bandwidth
of 10 MHZ.

(e) A two-stage Butterworth low-pass filter at the output
of multiplier stage can provide better high-frequency rejection

(f) Video amplifier can be replaced by one or two more
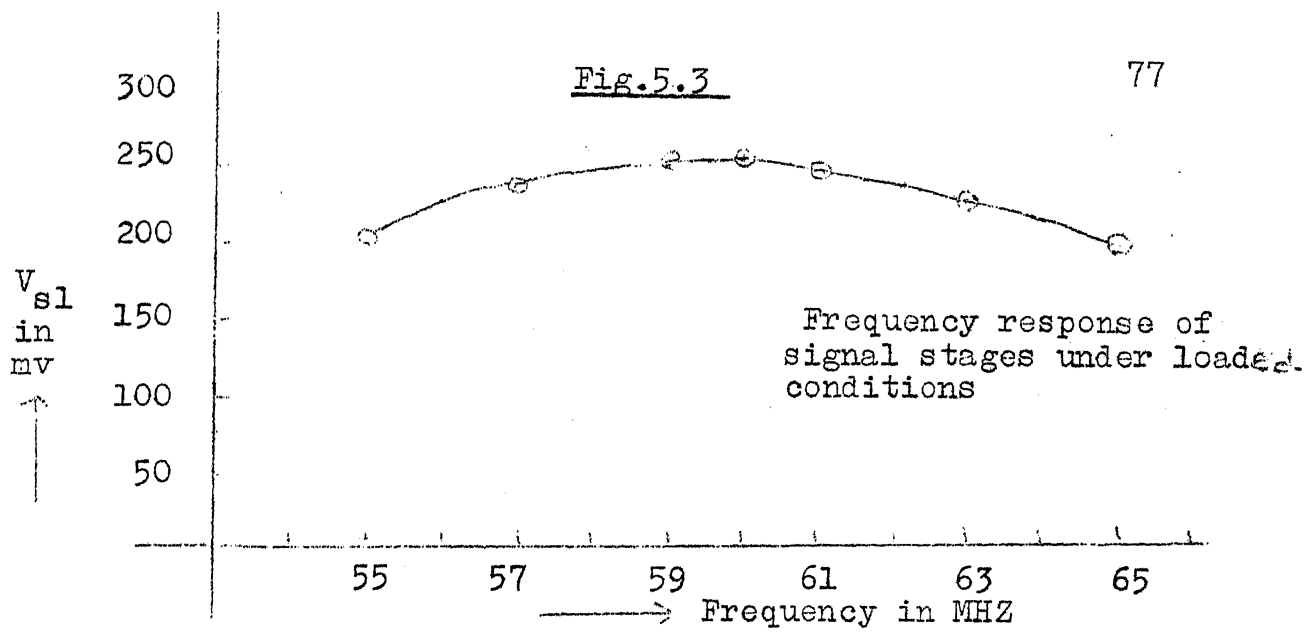stages of difference-amplifier before the comparator circuit.

Fig.5.3

Frequency response of
signal stages under loaded
conditions

V_{sl} in mv →

Frequency in MHZ

Fig.5.4

Frequency response
of system using
diffl-pair multiplier
using CA3028A.

V_{out} in mv

Freq. in MHZ

Fig. 5.5

Frequency response of
system using double balanc-
ed mixer using DBM-1.

V_{dem} in mv

Freq. in MHZ

APPENDIX-A

BRIEF MANUFACTURER'S SPECIFICATIONS OF DEVICES

Type	Max. Ratings				Ele. characteristics		
	V_{CB}	V_{CES}	V_{BE}	I_C	Conditions	h_{FE}	f_T
(1) 2N3324 PNP,Ge	35V	35V	3V	100ma	$V_{CE}=10V$, $I_C=3ma$	30 to 200	200 to 600 MHZ
(2) 2N918 NPN,Si	30V	15V	3V	50ma	$V_{CE}=10V$ $I_C=10ma$	20	960 MHZ
(3) 2N3563 NPN,Si	30V	12V			$I_C=8ma$	20 to 200	600 MHZ

(4) BFW10: (N-channel, silicon, JFET)

Gate-source voltage (open drain), $-V_{GSO}$ max $= 30V$

Feedback capacitance at 1 MHZ($V_{GS}=0$, $V_{DS}=15V$), $-C_{re} < 0.75pf$

Transfer admittance (common source) ($V_{GS}=0$, $V_{DS}=15V$),

$$Y_{FS} > 3.2 \text{ m mhos}$$

(5) SZ213: (Silicon expoxy, zener diode)

Nominal reference voltage, $V_{br} = 8.2V$

Max. dissipation at 25°C $= 250mw$

(6) CA3028A: (Linear IC)

It is a differential/cascode amplifier for operation at frequencies DC to 120 MHZ.

Elec. characteristics (at f=10.7MHZ, $V_{CC}=+9V$)

	Cascode	Diff.Amp
Y_{11}	0.6 + j 1.6 m $\sim$	0.5 + j0.5 m $\sim$
Y_{12}	0.0003-j0 "	0.01- j0.0002 m $\sim$
Y_{21}	99-j18. "	-37 + j0.5 "
Y_{22}	0 + j0.08 "	0.04 + j0.23 "

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